# SOME RESULTS ON RWW- AND RRWW-AUTOMATA AND THEIR RELATION TO THE CLASS OF GROWING CONTEXT-SENSITIVE LANGUAGES 

Tomasz Jurdziński ${ }^{1}$, Krzysztof Loryś ${ }^{2}$<br>Institute of Computer Science, University of Wroctaw<br>51-151 Wroctaw, Poland<br>e-mail: $\{\mathrm{tju}$, lorys $\}$ @ii. uni.wroc.pl<br>and<br>Gundula Niemann ${ }^{3}$, Friedrich Otto ${ }^{4}$<br>Fachbereich Mathematik/Informatik, Universität Kassel<br>D-34109 Kassel, Germany<br>e-mail: otto@theory.informatik.uni-kassel.de


#### Abstract

It is shown that already the RWW-automata of Jančar et al (1998) accept the Gladkij language $L_{\mathrm{Gl}}=\left\{w \# w^{R} \# w \mid w \in\{a, b\}^{*}\right\}$, which implies that the class GCSL of growing context-sensitive languages is a proper subclass of the class $\mathcal{L}(R W W)$ of languages accepted by the RWW-automata. In addition, it is shown that $\mathcal{L}(R W W)$ contains an NP-complete language. Also a simple reduction from the class $\mathcal{L}(R R W W)$ of languages accepted by the RRWW-automata to the class $\mathcal{L}(R W W)$ is presented, which indicates that these two classes will be hard to separate if they are not identical. Finally, characterizations of the class GCSL in terms of restricted versions of the RWW- and the RRWW-automata are given.


Keywords: Restarting automata, Gladkij language, growing context-sensitive languages

## 1. Introduction

A restarting automaton as described by Jančar, Mráz, Plátek and Vogel [6] is a nondeterministic machine model that processes strings which are stored in a list (or a 'rubber' tape). It has a finite control, and it has a read/write head with a finite lookahead working on the list of symbols. It performs two kinds of operations: move-right transitions, which shift the read/write head one position to the right changing the

[^0]
[^0]:    ${ }^{1}$ Currently visiting at the Fachbereich Mathematik/Informatik, Universität Kassel, supported by a grant from the Deutsche Forschungsgemeinschaft (DFG).
    ${ }^{2}$ The work of these two authors was partially supported by KBN, grant 8T11C 04419.
    ${ }^{3}$ Since July 2003 at SAP Deutschland.
    ${ }^{4}$ Corresponding author.

