# MEMBERSHIP FOR $k$-LIMITED ETOL LANGUAGES IS NOT DECIDABLE 

Henning Fernau ${ }^{1}$<br>Wilhelm-Schickard-Institut für Informatik, Universität Tübingen<br>Sand 13, D-72076 Tübingen, Germany<br>e-mail: fernauهinformatik.uni-tuebingen.de


#### Abstract

By the techniques developped in [1], we show how so-called $k$ lETOL machines can simulate register machines, hence proving that there are nonrecursive languages generable by $k$ lETOL systems (for each fixed $k \in \mathbb{N}$ ).


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## 1. Definition and Results

We proved [1] that there are nonrecursive languages generable by 1lEDT0L systems. In this note, we show that this result is also true in the more general case of $k$ IEDT0L systems (as introduced by WätJen [3]). In order to keep this note short, we refer the reader to our paper [1] as regards notations and definitions.

First, we generalize the notion of 11ET0L machine introduced in [1].
Definition 1 Let $k \geq 1$. A $k$ lETOL machine is given by $M=\left(V, V^{\prime},\left\{P_{1}, \ldots, P_{t}\right\}\right.$, $\{\sigma, x, y, R\})$, where $V, V^{\prime}=\{\sigma, y\},\left\{P_{1}, \ldots, P_{t}\right\}$ are the total alphabet, the terminal alphabet and the set of tables, respectively. $\sigma, x, y, R$ are special symbols in $V$. We say that $M$ computes the function $f: \mathbb{N}_{0} \longrightarrow \rightarrow \mathbb{N}_{0}$ iff the corresponding klETOL system $G_{M, n}=\left(V, V^{\prime},\left\{P_{1}, \ldots, P_{t}\right\}, x^{k n} R \sigma, k\right)$ with axiom $x^{k n} R \sigma$ generates a word of the form $y^{k m} \sigma$ if and only if $m=f(n)$. Especially, there is at most one word in $\{y\}^{*}\{\sigma\} \cap L\left(G_{M, n}\right)$.

Theorem 2 For any computable function $f: \mathbb{N}_{0} \longrightarrow \mathbb{N}_{0}$ and any $k \geq 1$, there exists a klETOL machine computing $f$.

Proof. $f: \mathbb{N}_{0} \longrightarrow \mathbb{N}_{0}$ can be described by an $r$-RMP (register machine program using $r$ registers) $P$. We describe a simulating $k$ lET0L machine $M=\left(V, V^{\prime}, H,\{\sigma, x, y, R\}\right)$ with

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V=\left\{\sigma, F, R, S, A_{1}, \ldots, A_{r}, y, C_{1}, \ldots, C_{r}\right\} \cup L \cup L^{\prime}
$$

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